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## Fourth Semester B.E. Degree Examination, Aug./Sept. 2020 Signals and Systems

Time: 3 hrs .
Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module. 2. Missing data, if any, may be suitably assumed.

## Module-1

1 a. Explain the following with an example each :
i) Even and odd signal
ii) Aperiodic and periodic signal
iii) Energy and power signal.
(06 Marks)
b. Sketch the following signal :
i) $\mathrm{y}(\mathrm{t})=\mathrm{r}(\mathrm{t}+2)-\mathrm{r}(\mathrm{t}+1)-\mathrm{r}(\mathrm{t}-1)+\mathrm{r}(\mathrm{t}-2)$
ii) $y(t)=r(t+2)-r(t+1)-r(t-1)+r(t-2)$
(06 Marks)
c. Verify the following properties of system :
memoryless, casual, stable and some invariant $\mathrm{y}(\mathrm{n})=\mathrm{nx}(\mathrm{n})$.
(08 Marks)

## OR

2 a. Sketch the even and odd parts of the signal shown in the Fig.Q2(a).


Fig.Q2(a)
(06 Marks)
b. Classify the following the following as an energy or power signal
i) $\mathrm{y}(\mathrm{t})=\mathrm{r}(\mathrm{t})-\mathrm{r}(\mathrm{t}-2)$
ii) $\mathrm{x}(\mathrm{t})=\left(1+\mathrm{e}^{-5 t}\right) \mathrm{u}(\mathrm{t})$.
(08 Marks)
c. Determine whether the following signals are periodic or not. If periodic find its fundamental time period.
i) $x[n]=5 \sin \left(\frac{7 \pi n}{12}\right)+8 \cos \left(\frac{14 \pi n}{8}\right)$
ii) $x(t)=\cos t+\sin \sqrt{2} t$.
(06 Marks)

## Module-2

3 a. Prove the following properties of convolution :
i) Commutative
ii) Distributive.
(06 Marks)
b. Determine the conyolution of the following two signals $x(t)=e^{-3 t} u(t)$ and $h(t)=u(t+2)$.
c. Find the convolution of the following sequences

$$
x(n)=\beta^{n} u(n) \text { with }|\beta|<1 \text { and } h(n)=u(n-3) \text {. }
$$

(07 Marks)

## OR

4 a. Determine the convolution sum of the given sequence $x(n)=\{1,2,3,1\}$ and $h(n)=\{1,2,1,-1\}$ sketch output.
(06 Marks)
b. The impulse response of the system is given by $h(t)=u(t)$. Determine the output of the system for an input $\mathrm{x}(\mathrm{t})=\mathrm{e}^{-\alpha \mathrm{t}} \mathrm{u}(\mathrm{t})$.
(08 Marks)
c. Prove the associative property of convolution.

## Module-3

5 a. Find the step response for the impulse response $h(t)=u(t+1)-u(t-1)$.
(06 Marks)
b. Find the overall impulse response of a cascade of two systems having identical impulse responses $h(t)=2[u(t)-u(t-1)]$.
(06 Marks)
c. Find the Fourier series coefficients $X(k)$ for the signal $x(t)=\sum_{m=-\infty}^{\infty}[\delta(t-1 / 2 m)]$. Sketch the magnitude and phase spectra.
(08 Marks)

## OR

6 a. Determine whether following system with the given impulse response is memoryless, causal and stable $h[n]=\left[\frac{1}{2}\right]^{\mathrm{n}} \mathrm{u}[\mathrm{n}]$.
(06 Marks)
b. Evaluate the DTFS representation for the signal $x(n)$ shown in Fig.6(b) and sketch its spectra.


Fig.Q6(b)
(08 Marks)
c. Find the Fourier series representation for the signal $X(t)=\sin (2 \pi t)+\cos (3 \pi t)$. Sketch the magnitude and phase spectra.
(06 Marks)

## Module-4

7 a. Prove the following properties of Fourier transform :
i) Time shifting
ii) Time domain convolution.
(08 Marks)
b. Find the Fourier transform of the signal.
c. Find the DTFT of the signal shown in the Fig.Q7(c).


Fig.Q7(c)
(06 Marks)

## OR

8 a. Explain the concept of sampling theorem and reconstruction of signals.
b. Find the DTFT of the sequence $x(n)=-a^{n} u[-n-1]$.
c. Find the Fourier transform of the signal $x(t)=e^{-3 t} u(t-1)$.
(06 Marks)

## Module-5

9 a. Explain the properties of ROC.
(05 Marks)
b. Find the Z-transform and the ROC of the discrete sinusoid signal.
$\mathrm{x}[\mathrm{n}]=[\sin (\Omega \mathrm{n})] \mathrm{u}[\mathrm{n}]$.
(07 Marks)
c. Find the transfer function and difference equation if the impulse response is
$\mathrm{h}[\mathrm{n}]=\left[\frac{1}{3}\right]^{\mathrm{n}} \mathrm{u}[\mathrm{n}]+\left[\frac{1}{2}\right]^{\mathrm{n}} \mathrm{u}[\mathrm{n}-1]$.
(08 Marks)

OR
10 a. Using power series expansion technique or long division method find the inverse $z$-transform of the following $\mathrm{X}(\mathrm{z})$.

$$
\text { i) } X(z)=\frac{z}{2 z^{2}-3 z+1} ; \operatorname{ROC}|z|<1 / 2
$$

ii) $\mathrm{X}(\mathrm{z})=\frac{\mathrm{z}}{2 \mathrm{z}^{2}-3 \mathrm{z}+1} ; \mathrm{ROC}|\mathrm{z}|>1$.
(08 Marks)
b. Determine the $z$-transform of the following signal $x[n]=2^{n} u[n]$.

Also obtain ROC and locations of poles and zeroes of X(z).
(06 Marks)
c. Using $z$-transform find the convolution of the following two sequences
$\mathrm{h}[\mathrm{n}]=\left\{\frac{1}{\uparrow}, \frac{1}{2}, \frac{1}{4}\right\}$ and
$\mathrm{x}[\mathrm{n}]=\delta[\mathrm{n}]+\delta[\mathrm{n}-1]+4 \delta(\mathrm{n}-2)$.

